

EE 105 Midterm-1 Solution

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$$q := 1.6 \cdot 10^{-19} \text{ C}$$

$$n_i := 10^{10} \text{ cm}^{-3}$$

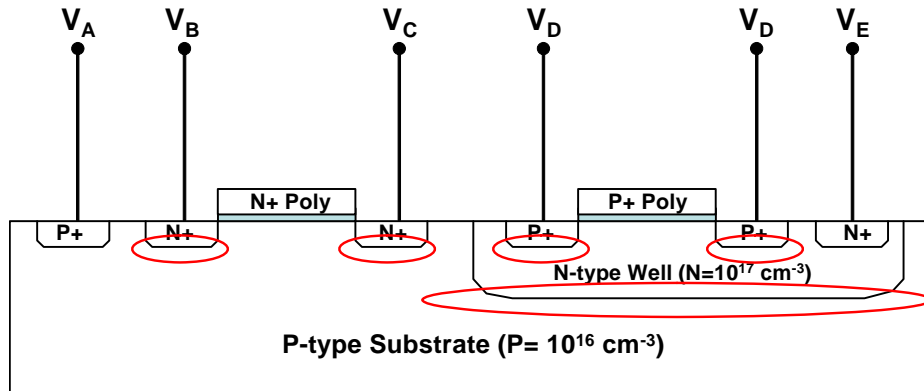
$$V_{th} := 0.026 \text{ V}$$

$$\epsilon_0 := 8.854 \cdot 10^{-14} \frac{\text{F}}{\text{cm}}$$

$$\epsilon_s := 11.7 \cdot \epsilon_0$$

$$\epsilon_{ox} := 3.9 \cdot \epsilon_0$$

(1)(a) There are 5 PN junctions



(b) V_A should be connected to the most negative voltage, or -2V , and V_E should be connected to the most positive voltage, or 2V , so that the N-well is reverse-biased

(2) (a) $N_d := 10^{16} \text{ cm}^{-3}$ $N_a := N_d$

$$\phi_n := 60 \text{ mV} \cdot \log\left(\frac{N_d}{n_i}\right) \quad \phi_p := -60 \text{ mV} \cdot \log\left(\frac{N_a}{n_i}\right)$$

$$\phi_{bi} := \phi_n - \phi_p \quad \phi_{bi} = 0.72 \text{ V}$$

(b)
$$x_d(V_d) := \sqrt{\frac{2 \cdot \epsilon_s \cdot (\phi_{bi} - V_d)}{q} \cdot \left(\frac{1}{N_a} + \frac{1}{N_d}\right)} \quad x_d(0) = 0.432 \text{ } \mu\text{m}$$

(c)
$$E_{max} := \frac{2 \cdot \phi_{bi}}{x_d(0)} \quad E_{max} = 3.335 \times 10^6 \frac{\text{V}}{\text{m}}$$

(d) The capacitance is inversely proportional to the depletion width:

$$C_{\text{ratio}} := \frac{x_d(-10\text{V})}{x_d(0)} \quad C_{\text{ratio}} = 3.859$$

(3) $\epsilon_d := 20 \cdot \epsilon_0$ $t_d := 1 \text{ nm}$ $N_d := 10^{16} \cdot \text{cm}^{-3}$

(a) $\phi_{pp} := -550 \text{ mV}$ $\phi_n := 60 \text{ mV} \cdot \log\left(\frac{N_d}{n_i}\right)$ $\phi_n = 0.36 \text{ V}$

$V_{FB} := -(\phi_{pp} - \phi_n)$ $V_{FB} = 0.91 \text{ V}$

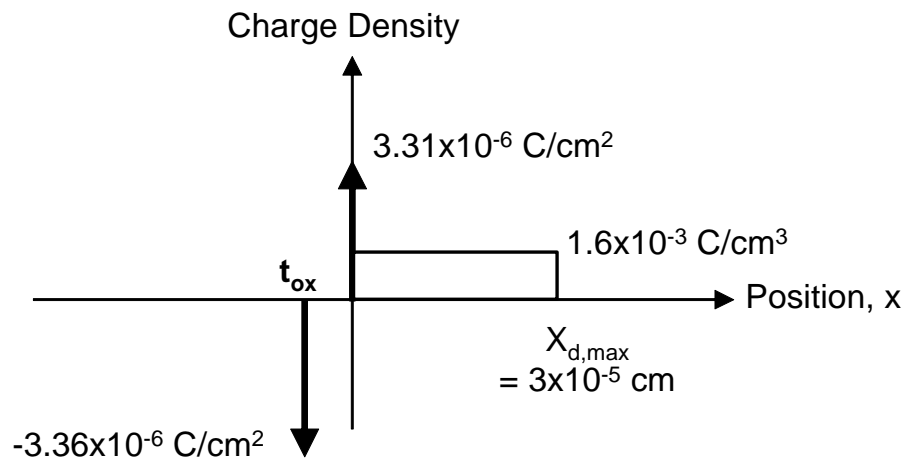
(b) $X_{d,max} := \sqrt{\frac{2 \cdot \epsilon_s \cdot (2 \cdot \phi_n)}{q \cdot N_d}}$ $X_{d,max} = 0.305 \text{ } \mu\text{m}$

$Q_{b,max} := q \cdot N_d \cdot X_{d,max}$

$C_d := \frac{\epsilon_d}{t_d}$

$V_{TH} := V_{FB} - 2 \cdot \phi_n - \frac{Q_{b,max}}{C_d}$ $V_{TH} = 0.187 \text{ V}$

(c)



(d) Since $0V < V_{TH}$, the PMOS is in inversion

$Q_b := Q_{b,max}$ $Q_b = 4.885 \times 10^{-8} \frac{\text{C}}{\text{cm}^2}$ $\frac{Q_b}{X_{d,max}} = 1.6 \times 10^{-3} \frac{\text{C}}{\text{cm}^3}$

$Q_c := -(0 - V_{TH}) \cdot C_d$ $Q_c = 3.316 \times 10^{-6} \frac{\text{C}}{\text{cm}^2}$

$Q_g := -(Q_b + Q_c)$ $Q_g = -3.365 \times 10^{-6} \frac{\text{C}}{\text{cm}^2}$

(d) $0V$ is in inversion, so the capacitance is equal to the capacitance of the dielectric

$C_d = 1.771 \times 10^{-5} \frac{\text{F}}{\text{cm}^2}$

$$(4) \quad \mu_{nCox} := 100 \cdot \frac{\mu A}{V^2} \quad \mu_{pCox} := 50 \cdot \frac{\mu A}{V^2} \quad \lambda_n := 0.05 V^{-1} \quad \lambda_p := 0.01 V^{-1}$$

$$V_{THn} := 1V \quad V_{THp} := -1V \quad V_{dd} := 5V \quad W_{over_L} := 10$$

$$(a) \quad I_d := 100 \mu A$$

$$V_x := 4V$$

Given

$$I_d = \frac{\mu_{pCox}}{2} \cdot W_{over_L} \cdot [(V_{dd} - V_x) - (|V_{THp}|)]^2$$

$$V_b := \text{Find}(V_x)$$

$$V_b = 3.368 V$$

$$V_y := 2V$$

Given

$$I_d = \frac{\mu_{nCox}}{2} \cdot W_{over_L} \cdot (V_y - V_{THn})^2$$

$$V_g := \text{Find}(V_y)$$

$$V_g = 1.447 V$$

$$(b) \quad g_{m1} := \sqrt{2 \cdot \mu_{pCox} \cdot W_{over_L} \cdot I_d}$$

$$g_{m1} = 3.162 \times 10^{-4} \frac{1}{\Omega}$$

$$r_{0_1} := \frac{1}{\lambda_p \cdot I_d}$$

$$r_{0_1} = 1 \times 10^6 \Omega$$

$$g_{m2} := \sqrt{2 \cdot \mu_{nCox} \cdot W_{over_L} \cdot I_d}$$

$$g_{m2} = 4.472 \times 10^{-4} \frac{1}{\Omega}$$

$$r_{0_2} := \frac{1}{\lambda_n \cdot I_d}$$

$$r_{0_2} = 2 \times 10^5 \Omega$$

$$(c) \quad A_v := -g_{m2} \cdot (r_{0_1}^{-1} + r_{0_2}^{-1})^{-1}$$

$$A_v = -74.536$$

(d) R_{in} is infinity

$$R_{out} := (r_{0_1}^{-1} + r_{0_2}^{-1})^{-1}$$

$$R_{out} = 1.667 \times 10^5 \Omega$$

(e) Maximum output voltage is reached when M_1 is at the edge of saturation

$$V_{out_max} := V_b + |V_{THp}|$$

$$V_{out_max} = 4.368 V$$

Minimum output voltage is reached when M_2 is at the edge of saturation

$$V_{out_min} := V_g - V_{THn}$$

$$V_{out_min} = 0.447 V$$

(f) The impedance looking into M_1 becomes

$$R_L := (g_{m1} + r_{0_1}^{-1})^{-1}$$

$$R_L = 3.152 \times 10^3 \Omega$$

$$A_v := -g_{m2} \cdot (R_L^{-1} + r_{o2}^{-1})^{-1}$$

$$A_v = -1.388$$

$$R_{out} := (R_L^{-1} + r_{o2}^{-1})^{-1}$$

$$R_{out} = 3.103 \times 10^3 \Omega$$

(g) $V_x := 2.5V$

Given

$$\frac{\mu_p C_{ox}}{2} \cdot W_{over_L} \cdot [(V_{dd} - V_x) - (|V_{THp}|)]^2 \cdot [1 + \lambda_p \cdot (V_{dd} - V_x)] = \frac{\mu_n C_{ox}}{2} \cdot W_{over_L} \cdot (V_y - V_x)^2$$

$V_{out} := \text{Find}(V_x)$

$$V_{out} = 2.518 V$$

$$V_{\text{THn}}^2 \cdot (1 + \lambda_n \cdot V_x)$$