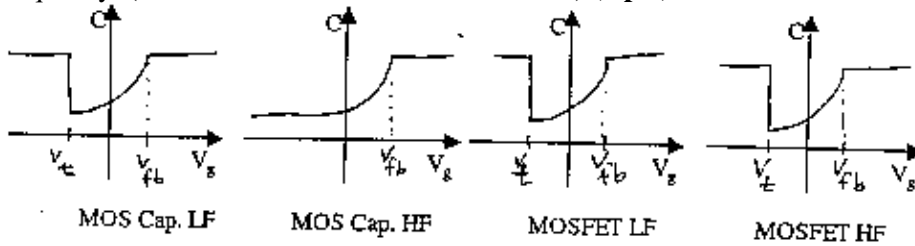


**EE 130, Spring/2000  
Midterm II Solutions  
Professor C. Hu**

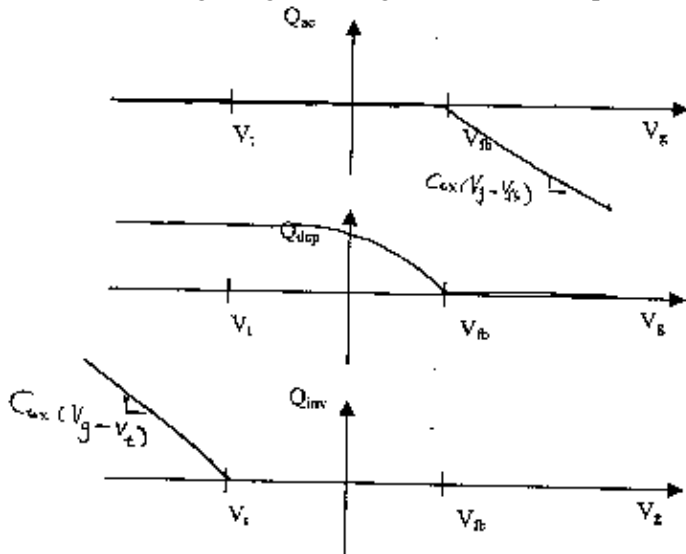
**Problem #1**

1. Consider a PMOSFET with a P+ poly-silicon gate and a N-type body. The body doping concentration is  $2.0 \times 10^{17} \text{ cm}^{-3}$ , and gate oxide thickness is 10nm. (35 Points)

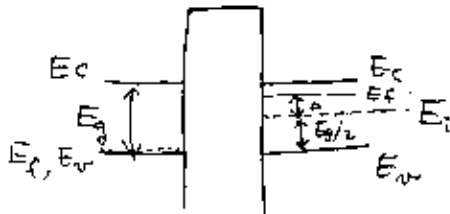
(a) Qualitatively sketch the C-V curve of MOS capacitor and MOSFET for high frequency and low frequency. (No need to calculate  $V_{fb}$  and  $V_t$  here) (7 pts)



(b) Draw charge vs gate voltage of PMOSFET qualitatively. (7 pts)



(c) Calculate the flat band voltage. (7 pts)



$$V_{fb} = E_g/2 + \Delta = E_g/2 + K \cdot T/q \cdot \ln(N_{sub}/N_i) = 0.55 + 0.026 \cdot \ln(2.0 \times 10^{17} / (1.0 \times 10^{10})) = 0.55 + 0.44 = 0.99V$$

(d) Calculate the threshold voltage. (7 pts)

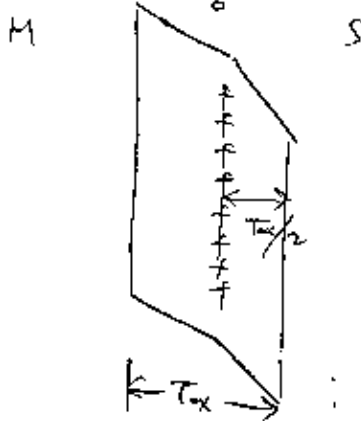
$$V_t = V_{fb} - 2\phi_{B} - \frac{\sqrt{2\epsilon_{Si}qN_{sub}}}{C_{ox}}$$

$$\phi_{B} = \sqrt{kT/q \ln(N_{sub}/N_1)} = 0.44 \text{ (} = \Delta \text{ in (d) )}$$

$$C_{ox} = \epsilon_{Si} / T_{ox} = 3.9 \times 8.85 \times 10^{-14} / 10^{-6} = 3.45 \times 10^{-7} \text{ (F/cm}^2\text{)}$$

$$V_t = 0.99 - 2 \times 0.44 - 2.41 \times 10^{-7} / (3.45 \times 10^{-7}) = -0.59 \text{ V}$$

(e) A sheet of electrons ( $6.9 \times 10^{-8} \text{ C/cm}^2$ ) is trapped at the center of the gate oxide. How much is the threshold voltage changed? (7 pts)

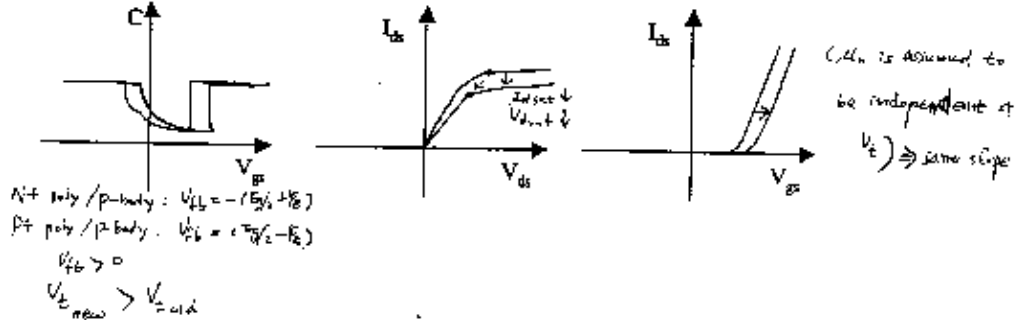


$$\Delta V_t = -Q / C_{oxe} = -Q / (\epsilon_{Si} / (T_{ox}/2)) = -Q / (2C_{ox}) = -(-6.9 \times 10^{-8}) / (2 \times 3.45 \times 10^{-7}) = 0.1 \text{ V}$$

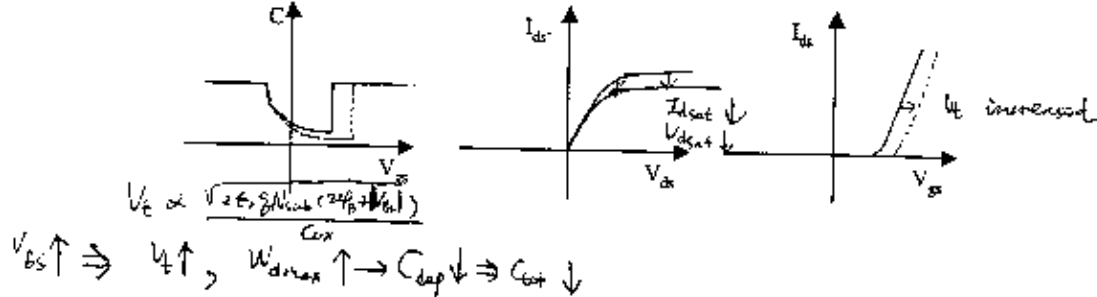
**Problem #2**

Qualitatively sketch the C-V, Id-Vg, and Id-Vd curves for an NMOSFET to indicate how the curves would differ in response to the changes given below. Assume the **mobility is fixed for (a) and (b)**. (30 pts)

(a) Change the poly-silicon gate from N+ to P+ type: (10 pts)

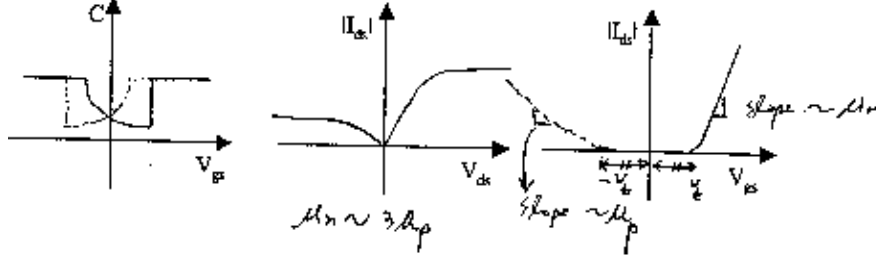


(b) Reverse back bias is applied to the body. (10 pts)



(c) Reverse the doping types of the source/drain, body, and gate, i.e. change from NMOSFET to PMOSFET. Select the proper quadrant. Source and body are tied to ground (0V). Consider  $\mu_n \neq \mu_p$ .

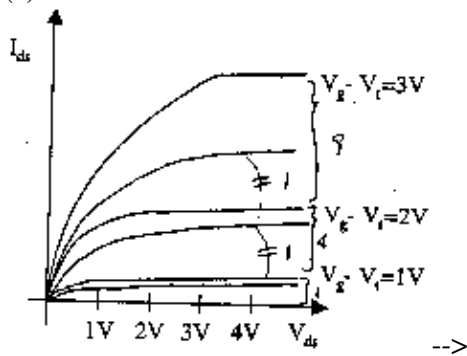
(10 pts)



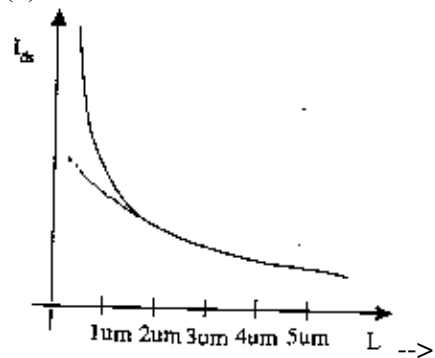
**Problem #3**

The printed curves in each of the figures are drawn for a MOSFET without consideration for velocity saturation. Draw new curves in each figure to indicate the effect of velocity saturation. (15 pts: 5 pts each)

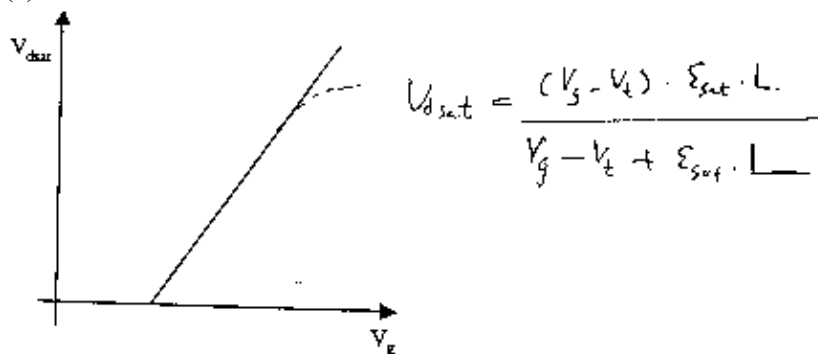
(a)



(b)



(c)



$V_{dsat} = (V_g - V_t) \cdot E_{sat} \cdot L / (V_g - V_t + E_{sat} \cdot L)$

**Problem #4**

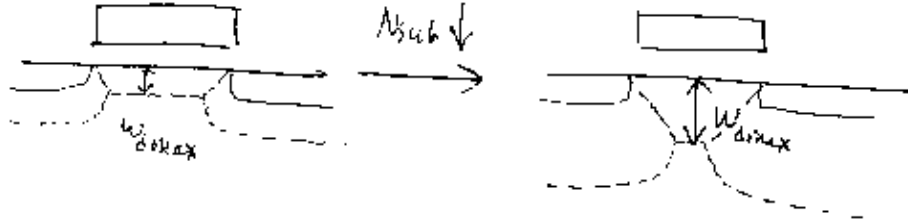
Indicate in the table below the consequences of decreasing the body doping concentration,  $N_{sub}$ , in an NMOSFET by checking two appropriate boxes (Increase/Decrease and Desirable/Undesirable) for each line. (20 pts)

	Increases	Decreases	Desirable	Undesirable	Points
Transconductance, $G_{m,sat}$	X		X		5 pts
Subthreshold swing, $S$		X	X		5 pts
$V_t$ roll-off (Short channel effect)	X			X	5 pts
Body effect coefficient, ALPHA		X	X		5 pts

i)  $G_{m,sat} = dI_{dsat}/dV_{gs} = \mu W C_{ox}/L * (V_g - V_t)$   $N_{sub}$  down implies  $V_t$  down implies  $G_{m,sat}$  up desirable

ii)  $S = 60mV * (1 + C_{dep}/C_{ox})$   $N_{sub}$  down implies  $W_{dmax}$  up implies  $C_{dep}$  down implies  $S$  down desirable

iii)



$V_t$  roll-off increases implies undesirable

iv)  $ALPHA = C_{dep}/C_{ox}$  ;  $N_{sub}$  down ;  $C_{dep}$  down ; ALPHA down

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