

# EECS 145L Final Examination Solutions (Fall 2002)

UNIVERSITY OF CALIFORNIA, BERKELEY  
College of Engineering, Electrical Engineering and Computer Sciences Department

- 1a Johnson noise** is produced by the thermal agitation of electrons in a resistor while shot noise arises from statistical fluctuations in the number of electrons per unit time
- 1b** The **sensor** transduces a physical quantity into an electrical signal and the **actuator** transduces an electrical signal into a physical quantity
- 1c** The **Thompson emf** is caused by a temperature gradient along the length of a conductor that causes the electrons to move to the colder end while the **Peltier emf** is produced when materials with two different electron mobilities are brought in contact and the electrons move to the material with the lower mobility.
- 1d** The **thermocouple** consists of two dissimilar wires joined at their ends and converts a temperature difference into a potential while the **Peltier thermoelectric heat pump** consists of a doped semiconductor and converts a current into a temperature difference
- 1e** The **EMG** is an electrical signal produced by skeletal muscle and has a random, noisy waveform while the **ECG** is an electrical signal produced by the heart muscle and consists of a periodic series of pulses.
- 1f** A **beta ray** is a moving electron while an **x-ray** is an energetic photon (typically 1-100 keV).  
[4 points off for not mentioning electron vs. photon]  
[4 points off for not mentioning difference in penetrating power]

**2a**

$$V_0 = V_1 \left( \frac{R_2 + R_3}{R_3} \right) \left( \frac{1/j\omega C}{1/j\omega C + R_1} \right) = V_1 \left( \frac{R_2 + R_3}{R_3} \right) \left( \frac{1}{1 + j\omega R_1 C} \right) = \left( \frac{R_2 + R_3}{R_3} \right) \left( \frac{1 - j\omega R_1 C}{1 + (\omega R_1 C)^2} \right)$$

$$\left| \frac{V_0}{V_1} \right| = \left( \frac{R_2 + R_3}{R_3} \right) \left( \frac{\sqrt{1 + (\omega R_1 C)^2}}{1 + (\omega R_1 C)^2} \right) = \left( \frac{R_2 + R_3}{R_3} \right) \left( \frac{1}{\sqrt{1 + (\omega R_1 C)^2}} \right)$$

- 2b** At 0 Hz, Gain = 10, so  $R_2 = 9 \text{ k}\Omega$  and  $R_3 = 1 \text{ k}\Omega$  is suitable  
Gain falls 3 dB to 7.07 at  $f = 1/(2\pi R_1 C) = 1 \text{ kHz}$ , so  $R_1 C = 0.159 \text{ ms}$   
Choosing  $R_1 = 10 \text{ k}\Omega$ , we have  $C = 0.0159 \text{ }\mu\text{F} = 15.9 \text{ nF}$

**2c**

$$\frac{V_1}{R_1} = -V_0 (1/R_2 + j\omega C)$$

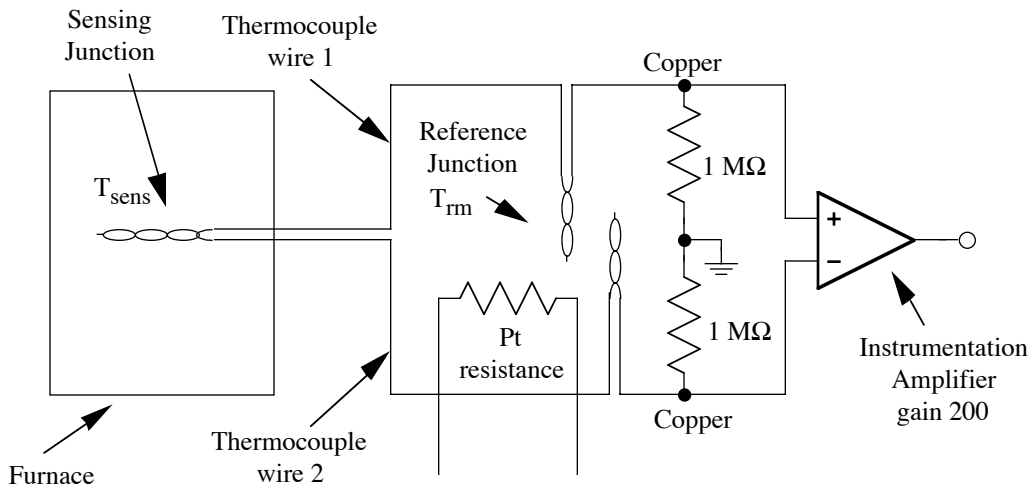
$$\frac{V_0}{V_1} = \frac{-1}{R_1 (1/R_2 + j\omega C)} = \frac{-R_2}{R_1} \left( \frac{1}{1 + j\omega R_2 C} \right) = \frac{-R_2}{R_1} \left( \frac{1 - j\omega R_2 C}{1 + (\omega R_2 C)^2} \right)$$

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$$\left| \frac{V_0}{V_1} \right| = \left( \frac{R_2}{R_1} \right) \left( \frac{\sqrt{1 + (\omega R_2 C)^2}}{1 + (\omega R_2 C)^2} \right) = \frac{(R_2/R_1)}{\sqrt{1 + (\omega R_2 C)^2}}$$

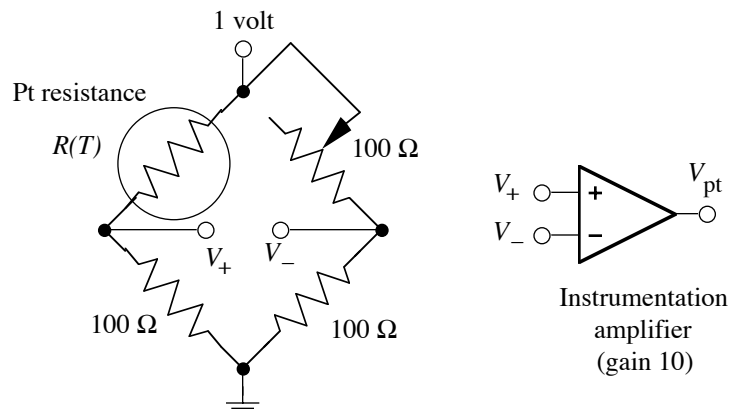
- 2d** At 0 Hz, Gain = 10, so  $R_1 = 10 \text{ k}\Omega$  and  $R_2 = 100 \text{ k}\Omega$  is suitable  
 Gain falls 3 dB to 7.07 at  $f = 1/(2\pi R_2 C) = 1 \text{ kHz}$ , so  $R_2 C = 0.159 \text{ ms}$   
 Since  $R_2 = 100 \text{ k}\Omega$ , we have  $C = 0.00159 \text{ }\mu\text{F} = 1.59 \text{ nF}$

**3a**



[6 points off for no instrumentation amplifier]

**3b**



[6 points off for no instrumentation amplifier]

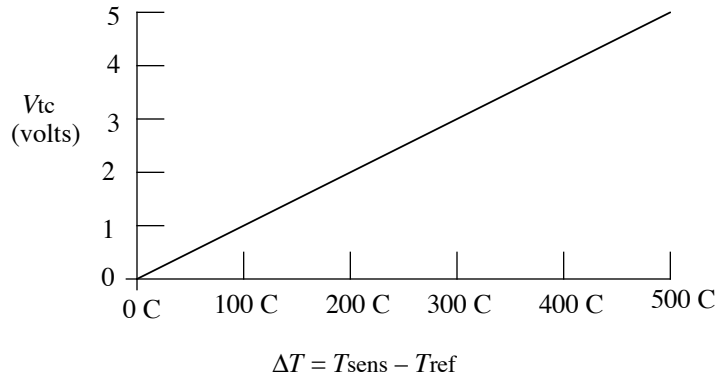
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$$V_+ - V_- = \frac{100}{100 + 100(1 + 0.004T)} - \frac{100}{200} = \frac{1}{2 + 0.004T} - \frac{1}{2}$$

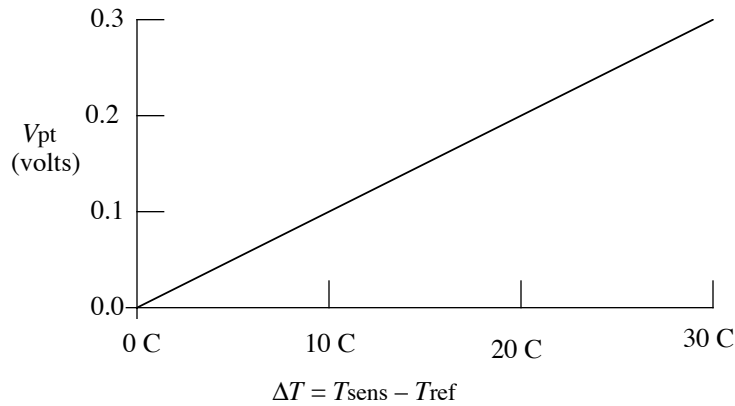
$$= \frac{0.5}{1 + 0.002T} - \frac{0.5}{1} \approx 0.5(1 - 0.002T) - 0.5 = 0.001T \text{ (volts)}$$

The bridge sensitivity is 1 mV /C° and a gain of 10 is needed to increase the sensitivity to 10 mV/C°.

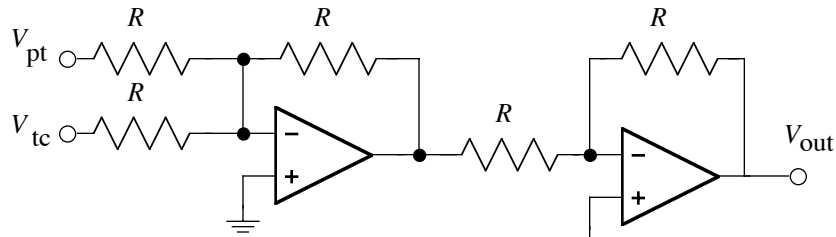
3c



3d



3e



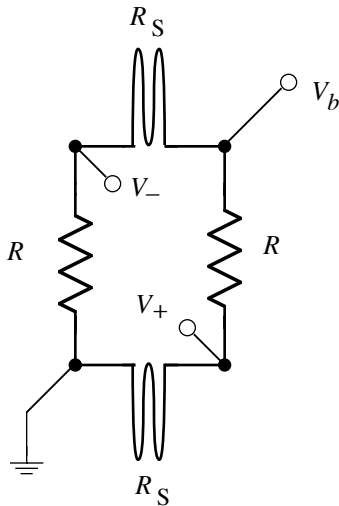
$$V_{\text{out}} = V_{\text{tc}} + V_{\text{pt}}$$

R = 1 kΩ would be suitable

[3 points off for subtracting  $V_{\text{tc}}$  and  $V_{\text{pt}}$  rather than adding.]

[1 point off for  $V_{\text{out}} = -V_{\text{pt}} - V_{\text{tc}}$ ]

4a



4b  $R = 100 \Omega$

$$R_S = R + \Delta R$$

$$V_+ - V_- = V_b \left[ \frac{R + \Delta R}{\Delta R + 2R} - \frac{R}{\Delta R + 2R} \right] =$$

$$V_b (\Delta R) / (\Delta R + 200) \approx V_b \Delta R / (2R)$$

4c Voltage across each strain gauge  $\approx V_b / 2$  (since  $\Delta R \ll R$ )

$$\text{Power} = (V_b / 2)^2 / 100 \Omega < 0.25 \text{ W}$$

want highest  $V_b$  for sensitivity but power limits  $V_b < 10$  volts (5 volts was accepted)

[6 points off for "does not matter"]

[4 points off for 1V and not considering max power]

4d  $\Delta T = 1 \text{ }^\circ\text{C}$  means  $\Delta L/L = 23 \text{ ppm}$  and  $\Delta R/R = 46 \text{ ppm}$ .

$$V_+ - V_- = (10 \text{ volts})(23 \text{ ppm}) = 230 \mu\text{V}/^\circ\text{C}$$

(115  $\mu\text{V}/^\circ\text{C}$  for 5 V bias)

4e noise is 10  $\mu\text{V}$  at 1 MHz-  $\Delta T = 1/23 \text{ }^\circ\text{C} = 43 \times 10^{-3} \text{ }^\circ\text{C}$

noise is 10 nV at 1 Hz  $\Delta T = 1/23,000 \text{ }^\circ\text{C} = 43 \times 10^{-6} \text{ }^\circ\text{C}$

## EECS 145L Final Examination Solutions (Fall 2002)

145L Final Examination score distribution:

70-79    0	80-89    1	90-99    0
100-109 0	110-119 0	120-129 0
130-139 1	140-149 1	150-159 4
160-169 1	170-179 3	180-189 5
190-199 7	200    1	

19 undergraduates: average = 173.4, rms = 26.0

5 other students (1 graduate, 2 extension, 2 exchange) : average = 176.0, rms = 21.0

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### 145L Course Grade Distribution

Grade	Undergraduate Scores	Other Scores
<b>A+</b>	974	982
<b>A</b>	950, 952, 960, 972	
<b>A-</b>	918, 923, 923, 927, 938, 940	913, 923, 932
<b>B+</b>	901, 907	895
<b>B</b>	869, 873, 881	
<b>B-</b>	835, 844	
<b>C+</b>		
<b>C</b>		
<b>C-</b>		
<b>D+</b>		
<b>D</b>		
<b>D-</b>		
<b>F</b>	463	
Maximum	1000	1000
Average	892.0	929.0
rms	111.5	32.7