

LAST Name _____ FIRST Name _____

Lab Time _____

- **(10 Points)** Print your name and lab time in legible, block lettering above AND on the last page where the grading table appears.
- This exam should take up to 70 minutes to complete. You will be given at least 70 minutes, up to a maximum of 80 minutes, to work on the exam.
- **This exam is closed book.** Collaboration is not permitted. You may not use or access, or cause to be used or accessed, any reference in print or electronic form at any time during the exam, except one double-sided 8.5" × 11" sheet of handwritten notes having no appendage. Computing, communication, and other electronic devices (except dedicated timekeepers) must be turned off. Noncompliance with these or other instructions from the teaching staff—including, for example, commencing work prematurely or continuing beyond the announced stop time—is a serious violation of the Code of Student Conduct. Scratch paper will be provided to you; ask for more if you run out. You may not use your own scratch paper.
- **The exam printout consists of pages numbered 1 through 6.** When you are prompted by the teaching staff to begin work, verify that your copy of the exam is free of printing anomalies and contains all of the six numbered pages. If you find a defect in your copy, notify the staff immediately.
- Please write neatly and legibly, because *if we can't read it, we can't grade it.*
- For each problem, limit your work to the space provided specifically for that problem. *No other work will be considered in grading your exam. No exceptions.*
- Unless explicitly waived by the specific wording of a problem, you must explain your responses (and reasoning) succinctly, but clearly and convincingly.
- We hope you do a *fantastic* job on this exam.

MT1.1 (30 Points) The input-output behavior of a continuous-time system is described by the following equation:

$$y(t) = \begin{cases} 0 & \text{if } x(t) \leq 0 \\ x(t) & \text{if } x(t) > 0, \end{cases}$$

where x denotes the input and y the output. For each part, explain your reasoning succinctly, but clearly and convincingly.

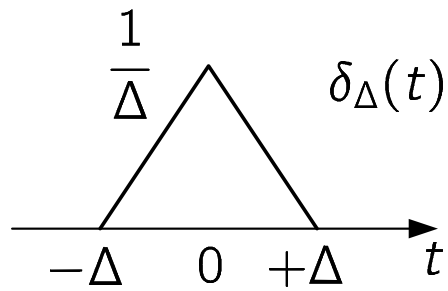
(a) (15 Points) Select the strongest true assertion from the list below.

- (i) The system must be linear.
- (ii) The system could be linear, but does not have to be.
- (iii) The system cannot be linear.

(b) (15 Points) Select the strongest true assertion from the list below.

- (i) The system must be time invariant.
- (ii) The system could be time invariant, but does not have to be.
- (iii) The system cannot be time invariant.

MT1.2 (55 Points) Consider the continuous-time signal δ_Δ shown below.



We know that in the limit $\Delta \rightarrow 0$, the triangular pulse behaves like a unit-strength Dirac delta. In this problem, you will explore the behavior of $\dot{\delta}_\Delta(t) \triangleq d\delta_\Delta(t)/dt$.

- (a) (10 Points) Provide a well-labeled plot of $\dot{\delta}_\Delta(t)$; you must explain briefly how you determine each salient feature of the plot.

- (b) (15 Points) Consider a smooth test function g . Provide a reasonable approximation (in terms of g) to the following integral:

$$\int_{-\infty}^{+\infty} g(t) \delta_{\Delta}(t) dt.$$

You may find the trapezoidal approximation rule from calculus helpful.

- (c) (15 Points) Let $\dot{\delta}(t) = \lim_{\Delta \rightarrow 0} \dot{\delta}_{\Delta}(t)$. Explain why the following equality is correct:

$$\int_{-\infty}^{+\infty} g(t) \dot{\delta}(t) dt = -\dot{g}(0).$$

- (d) (15 Points) Use the result of part (c) to evaluate the integral

$$\int_{-\infty}^{+\infty} g(\tau) \dot{\delta}(t - \tau) d\tau.$$

MT1.3 (20 Points) Determine and provide a well-labeled plot containing each of the 4th roots of $z = \frac{16}{\sqrt{2}} + i\frac{16}{\sqrt{2}}$; be sure to draw the unit circle so the positions of the roots relative to it are clear. Also, determine the sum of all the fourth roots.

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Problem Name	Points	Your Score
1	30	
2	55	
3	20	
Total	115	