These solutions are in beta! Please post corrections as a follow-up to the Piazza post.

UC Berkeley – Computer Science
CS61B: Data Structures

Midterm #1, Spring 2018

This test has 7 questions worth a total of 160 points, and is to be completed in 110 minutes. The exam is closed book, except that you are allowed to use one double sided written cheat sheet (front and back). No calculators or other electronic devices are permitted. Give your answers and show your work in the space provided. **Write the statement out below in the blank provided and sign. You may do this before the exam begins.**

"I have neither given nor received any assistance in the taking of this exam."

Meow meow meow meow meow mooo meow meow purr.

Signature: Nibbles

#	Points	#	Points
0	0.75	6	20
1	19	7	23
2	12		
3	16.25		
4	39		
5	30		
		TOTAL	160

Name: Nibbles

SID: 8675309

Three-letter Login ID: nib

Login of Person to Left: jos

Login of Person to Right: hug

Exam Room: 779 Soda

Tips:

- There may be partial credit for incomplete answers. Write as much of the solution as you can, but bear in mind that we may deduct points if your answers are much more complicated than necessary.
- There are a lot of problems on this exam. **Work through the ones with which you are comfortable first. Do not get overly captivated by interesting design issues or complex corner cases you're not sure about.**
- Not all information provided in a problem may be useful.
- Unless otherwise stated, all given code on this exam should compile. All code has been compiled and executed before printing, but in the unlikely event that we do happen to catch any bugs in the exam, we'll announce a fix. Unless we specifically give you the option, the correct answer is not 'does not compile.'
- ○ indicates that only one circle should be filled in.
- ☐ indicates that more than one box may be filled in.
- For answers which involve filling in a ○ or ☐, please fill in the shape completely.
- When the exam says "write only one statement per line", a for loop counts as one statement.

Optional. Mark along the line to show your feelings on the spectrum between ☹ and ☺.
Before exam: [☹ x ☺].
After exam: [☹ x ☺].

Clarifications:

`4c. Removes all y from x. Returns first node in x that is not y. May not use new. Destructive.` **`This is just a clarification and does not change the problem.`**

`6b. ...the method below so that it ~~prints out~~` **`returns`**

`7b. There should not be an @Override tag.`

`7b. You can assume x is non-null.`

One of your TAs, Kevin Lin, has made wonderful walkthrough videos for you:
https://www.youtube.com/playlist?list=PLnp31xXvnfRqAfvA4R9Oh09PstFymwCif

0. So it begins (0.75 points). Write your name and ID on the front page. Write the exam room. Write the IDs of your neighbors. Write the given statement. Sign when you're done with the exam. Write your login in the corner of every page. Enjoy your free ~~half~~ ¾ point ☺.

1. Static Dada.

a) **(10 points)** Consider the class shown below. Next to the lines with blanks, write the result of the print statement. **No syntax errors or runtime errors occur.**

```
public class Dada {
    private Dada[] r;
    private static Dada[] rs;
    private String name;
    public Dada(String n) { name = n; }
    /** Prints out the given array, i.e. if d contains two Dadas
     *  with names "alice" and "bob", this method will print "alice bob". */
    private static void printDadaArray(Dada[] d) {
        for (int i = 0; i < d.length; i += 1) {
            System.out.print(d[i].name + " "); }
        System.out.println();
    }
    public static void main(String[] args) {
        Dada a = new Dada("alice");       // reminder from lecture:
        Dada b = new Dada("bob");         // twod = {{a, b}, {c, d}} creates
        Dada c = new Dada("carol");       // an array of Dada arrays where
        Dada d = new Dada("dan");         // the first array contains {a, b}
        Dada[][] twod = {{a, b}, {c, d}}; // and the second {c, d}
        a.r = twod[1];
        printDadaArray(a.r);              // carol dan
        Dada.rs = a.r;
        b.r = Dada.rs;
        b.r = new Dada[]{d, c};
        Dada.rs[1] = new Dada("eve");
        printDadaArray(Dada.rs);          // carol eve
        printDadaArray(b.r);              // dan carol
        printDadaArray(twod[0]);          // alice bob
        printDadaArray(twod[1]);          // carol eve
    }
}
```

b) **(9 points)** Suppose we add new methods to `Dada` called `fillOne` and `fillMany` and replace main as shown below. Fill in the print statements. The Dada class is otherwise unchanged.

```
private static void fillMany(Dada[] d) {
    System.arraycopy(rs, 0, d, 0, d.length);
    // Reminder, arraycopy parameters are:
    // (Dada[] from, int start, Dada[] to, int destination, int num)
}

private static void fillOne(Dada d) {
    d = rs[0];
}

public static void main(String[] args) {
    Dada a = new Dada("alice");
    Dada b = new Dada("bob");
    Dada c = new Dada("carol");
    Dada d = new Dada("dan");
    Dada[][] twod = {{a, b}, {c, d}};

    Dada.rs = new Dada[]{new Dada("fritz"), new Dada("gritz")};
    c.r = twod[0];
    printDadaArray(c.r);          // alice bob
    fillOne(c.r[0]);
    printDadaArray(c.r);          // alice bob
    fillMany(c.r);
    printDadaArray(c.r);          // fritz gritz
}
```

For your convenience, the instance variables of `Dada` were:

```
private Dada[] r;
private static Dada[] rs;
private String name;
```

2. What It Do (12 Points).

a) Consider the code below.

```
public static int f(int x) {
    if (x == 1) {
        return 1;
    }
    return 2 * f(x / 2);
}
```

Describe as **succinctly** as possible what this method does when executed for **all possible values of x.** If the behavior is different depending on x, describe the behavior in every interesting case. Remember that integer division in Java rounds down, i.e. 3/2 yields 1.

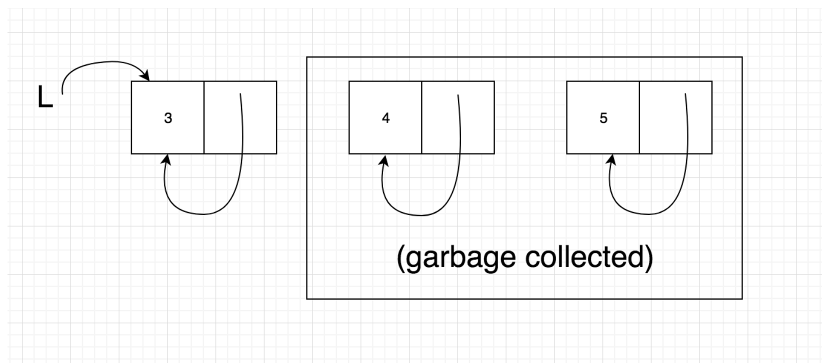
For x >= 1, prints out the largest power of 2 that is smaller than x. For x < 1, goes into infinite loop.

b) Consider the code below.

```
public static void g(IntList x) {
     if (x == null) { return; }
     g(x.rest);
     x.rest = x;
}
```

Draw a box and pointer diagram that shows the result of executing the following two lines of code. If any objects are not referenced by anything else (i.e. are garbage collected), you may omit drawing them if you prefer. If you need it, the `IntList` definition is on page 7. If `g` never finishes because it gets stuck in an infinite loop, write "Infinite Loop" instead of drawing a diagram.

```
IntList L = IntList.of(3, 4, 5); //creates an IntList containing 3, 4, and 5
g(L);
```



3. **KeyGate (16.25 points)**. Suppose we have the classes defined below, with 3 lines marked with **UK**, **USK**, and **UF**.

```
public class FingerPrint {...}
public class Key { ... }
public class SkeletonKey extends Key { ... }

public class StandardBox {  public void unlock(Key k) { ... }  } // UK

public class BioBox extends StandardBox {
    public void unlock(SkeletonKey sk) {  }                      // USK
    public void unlock(Fingerprint f) {  }                       // UF
}
```

For each line below, fill in exactly one bubble. **If a line causes an error, assume it is commented out before the following lines are run.**

```
public void doStuff(Key k, SkeletonKey sk, Fingerprint f) {
    StandardBox sb = new StandardBox();
    StandardBox sbbb = new BioBox();
    BioBox bb = new BioBox();
```

	Compile Error	Runtime Error	UK Runs	USK Runs	UF Runs
`sb.unlock(k);`	○	○	○ (red)	○	○
`sbbb.unlock(k);`	○	○	○ (red)	○	○
`bb.unlock(k);`	○	○	○ (red)	○	○
`sb.unlock(sk);`	○	○	○ (red)	○	○
`sbbb.unlock(sk);`	○	○	○ (red)	○	○
`bb.unlock(sk);`	○	○	○	○ (red)	○
`sb.unlock(f);`	○ (red)	○	○	○	○
`sbbb.unlock(f);`	○ (red)	○	○	○	○
`bb.unlock(f);`	○	○	○	○	○ (red)
`bb = (BioBox) sbbb;`	○	○	← Leave blank if no error		
`((StandardBox) bb).unlock(sk);`	○	○	○ (red)	○	○
`((StandardBox) sbbb).unlock(sk);`	○	○	○ (red)	○	○
`((BioBox) sb).unlock(sk);`	○	○ (red)	○	○	○

```
}
```

4. **Sans**. Implement the methods below. For reference, the `IntList` class is defined on the following page.

a) **(9 points).** `/** Non-destructively creates a copy of x that contains no y. */`

```
    public static int[] sans(int[] x, int y) {
        int[] xfirst = new int[x.length];
        int c = 0;
        for (int i = 0; i < x.length; i += 1) {
            if (x[i] != y) {
                xfirst[c] = x[i];
                c = c + 1;
            }
        }
        int[] r = new int[c];
        System.arraycopy(xfirst, 0, r, 0, c);
        return r;
    }
```

b) **(9 points).** `/** Non-destructively creates a copy of x that contains no y. */`

```
    public static IntList ilsans(IntList x, int y) {
        if (x == null) {
            return null;
        }
        if (x.first == y) {
            return ilsans(x.rest, y);
        }
        return new IntList(x.first, ilsans(x.rest, y));
    }
```

c) **(9 points).** `/** Destructively creates a copy of x that contains no y. You may not use` **`new`**`. */`

```
    public static IntList dilsans(IntList x, int y) {
        if (x == null) {
            return null;
        }
        x.rest = dilsans(x.rest, y);
        if (x.first == y) {
            return x.rest;
        }
        return x;
    }
```

d) (12 points). Suppose we want to write tests for `ilsans` and `sans`. Fill in the code below with a JUnit test that each method behaves as expected for one example input. Do not write a test for null inputs. Reminder that `IntList.of(4, 5, 6)` creates an `IntList` containing the values 4, 5, and 6. Assume the methods on the previous page are all part of a class called `Sans`, i.e. they are invoked as `Sans.sans`.

```
import org.junit.Test;
import static org.junit.Assert.*;
public class TestSans {
    @Test
    public void testSans() {  // TEST THE ARRAY VERSION OF SANS
        int[] x = {1, 2, 3, 4, 5, 6, 2, 2, 3, 3};
        int y = 2;
        int[] expected = {1, 3, 4, 5, 6, 3, 3};
        int[] actual = sans(x, y);
        assertArrayEquals(expected, actual);
}

    @Test // TEST THE NON-DESTRUCTIVE INTLIST VERSION OF SANS
    public void testIlsans() {
        IntList x = IntList.of(1, 2, 3);
        int y = 2;
        IntList expected = IntList.of(1, 3);
        IntList actual = Sans.ilsans(x, y);
        assertEquals(expected, actual);
        assertNotEquals(x, actual); // x should not have been altered
}
```

For reference, part of the `IntList` class definition is given below:

```
public class IntList {
    public int first;
    public IntList rest;
    public IntList(int f, IntList r) {
        first = f;
        rest = r;
    }
    public IntList() {}
    public static IntList of(Integer... args) { /* works correctly */ }
    public boolean equals(Object x) { /*works correctly w/ assertEquals*/ }
}
```

5. A Needle in ArrayStack. The Stack interface is given below. A Stack is basically like the proj1 Deque, where push is like "addLast", and pop is like "removeLast". For example, if we call `push(5)`, `push(10)`, `push(15)`, then call `pop()`, we'd get 15. If we call `pop()` again, we get 10.

```
public interface Stack<Item> {
    void push(Item x); // places an item on "top" of the stack
    Item pop();        // removes and returns "top" item of the stack
    int size();        // returns the number of items on the stack
}
```

a) **(14 points).** Fill in the `ArrayStack` implementation below. To ensure efficient memory usage, double the array size when full, halve the array size when < ¼ full, and avoid storing unnecessary references. The if conditions for resizing during `push` and `pop` are provided for you.

```
 public class ArrayStack<Item> implements Stack<Item> {
    private Item[] items;
    private int size;

    public ArrayStack() { // initial array size should be 8
        items = (Item[]) new Object[8];
        size = 0;
    }
    private void resize(int capacity) {
        Item[] newItems = (Item[]) new Object[capacity];
        System.arraycopy(items, 0, newItems, 0, size);
        items = newItems;
    }

    public void push(Item x) {
        if (usage_ratio() == 1) { resize(size * 2); }
        items[size] = x;
        size += 1;
    }

    public Item pop() {
        if (size == 0) {  return null; }
        if (usage_ratio() < 0.25 && items.length > 8) {resize(items.length / 2);}
        size = size - 1;
        Item returnItem = items[size];
        items[size] = null;
        return returnItem;
    }
    public int size() { return size; }
    private double usage_ratio() { return ((double) size()) / items.length; }
}
```

b) **(18 points)** Suppose we want to add a **default method** `purge(Item x)` **to the `Stack` interface** that eliminates all instances of x from the `Stack`, but leaves the stack otherwise unchanged. When comparing two items, remember to use `.equals` instead of `==`. You may not assume items are non-null.

For example, suppose if we create a Stack and call `push(1)`, `push(2)`, `push(3)`, `push(2)`, `push(2)`, `push(2)`, then call `purge(2)`, the stack would be reduced to size 2, and would have 3 on top and 1 on the bottom.

You may use an `ArrayStack`. For this problem and assume it works correctly, even if you didn't finish part a or are unsure of your answer. **You may not explicitly instantiate any other class or any array of any kind**, e.g. no `new LinkedListDeque<>(), new int[]`, etc.

```
public interface Stack<Item> {
    void push(Item x);
    Item pop();
    int size();
    default void purge(Item x) {
        if (size() == 0) {
            return;
        }
        Item top = pop();
        purge(x);
        if (!x.equals(top)) {
            push(top);
        }
    }
}

Or less elegant solution:

    ArrayStack<Item> as = new ArrayStack<>();
    while (size() > 0) {
        Item next = pop();
        if (!x.equals(next)) {
            as.push(next);
        }
    }
    while (as.size() > 0) {
        push(as.pop());
    }
```

Midterm 1 Leisure Region. Please relax and have a nice time in this region.
Nibbles is hoping that you're having a good time. -->

6. **Combine.** The `Combine.combine` method takes a `ComFunc` and an integer array x and uses the `ComFunc` to "combine" all the items in x. For example, if we have an implementation of `ComFunc` called `Add` that adds two integers, and we call `combine` using the `Add` class on the array {1, 2, 3, 4}, the result will be 10, since 1 + 2 + 3 + 4 is 10.

a) **(16 points).** Fill in the `combine` method below. If the array is of length 0, the result should be 0, and if the array is of length 1, the result should be the number in the array. For full credit use recursion. For 75% credit, you may use iteration. **<u>You may create a private helper function in the space provided.</u>**

```
public interface ComFunc {
  int apply(int a, int b); // apply(a, b) must equal apply(b, a)
}
public class Combine {
    public static int combine(IntBinaryFunction f, int[] x) {
        if (x.length == 0) {
            return 0;
         }
         if (x.length == 1) {
             return x[0];
         }
         int t = f.apply(x[0], x[1]);
         return combine(f, x, t, 2);
    }

    private static int combine(IntBinaryFunction f, int[] x, int t, int k) {
        if (k == x.length) {
            return t;
        }
        t = f.apply(x[k], t);
        return combine(f, x, t, k + 1);
    }

Or less elegant solution:
    private static int combineAlt(IntBinaryFunction f, int[] x) {
        int t = f.apply(x[0], x[1]);
        for (int i = 2; i < x.length; i += 1) {
            t = f.apply(x[i], t);
        }
        return t;
    }
```

b) **(4 points).** Suppose we have a method that adds two numbers, as shown below.

```
public class Add implements ComFunc {
  public int apply(int a, int b) {
    return a + b;
```

```
  }
}
```

Fill in the method below so that it prints out the correct result. You may use your answer from part a. Even if you left part a blank or think it be incorrect, you can assume that everything works as expected.

```
public static int sumAll(int x[]) { // sumAll is not a member of Combine
  return Combine.combine(new Add(), x);
}
```

7. The Downside of Default. Consider the `ListOfInts` interface below. `addLast`, `get`, and `size` behave exactly as your Deque interface from project 1A. `set(int i, int value)` sets the ith integer in the list equal to value. `plusEquals` adds each int in x to the corresponding int in the current list, i.e. if we call have a list L = [2, 3, 4] and we call `L.plusEquals([5, 6, 7])`, then after the call is complete, L will contain the values [7, 9, 11]. **If the lists are not of the same length, `plusEquals` should have no effect**.

a) **(6 points).** Fill in the `plusEquals` method below.

```
public interface ListOfInts {
    public void addLast(int i);
    public int get(int i);
    public int size();
    public void set(int i, int value);
    default public void plusEquals(ListOfInts x) { // assume x is non-null
        if (this.size() != x.size()){ return; }
        for (int i = 0; i < size(); i += 1) {
            this.set(i, this.get(i) + x.get(i));
        }
    }
}
```

b) **(10 points).** The `DLListOfInts` class stores a doubly linked list of integers, similar to your LinkedListDeque class. Assume that the list has a single sentinel node that points at itself when the list as empty, just like in lecture and in the recommended approach for proj1a. Fill in the `plusEquals` method so that it behaves as in part a. You must use iteration. You cannot call `super.plusEquals`.

```
public class DLListOfInts implements ListOfInts {
    public class IntNode {
        public int item;
        public IntNode next, prev;
    }

    private IntNode sentinel;
    private int size;

    public void plusEquals(DLListInt x) {
        if (x == null || this.size() != x.size()) {
            return;
        }

        IntNode xPtr = x.sentinel.next;
        for (IntNode p = sentinel.next; p != sentinel; p = p.next) {
            p.item += xPtr.item;
            xPtr = xPtr.next;
        }
    } ...
```

c) **(7 points)** The method `sumOfLists` given below is supposed to take an array of `DLListOfInts` and returns a `DLListOfInt` that is equal to the element-wise sum of all of the lists. For example if the array contains three lists that hold [2, 2, 2], [1, 2, 3], and [3, 3, 3], respectively, the method should return a `DLListOfInts` that contains [6, 7, 8]. The method should be non-destructive.

```
public class PartC {
      /** Non-destructively computes the sum of the given lists. Assumes
        * that all lists are of the same length and that none are null. */
      public static DLListOfInts sumOfLists(DLListOfInts[] lists) {
          ListOfInts result = lists[0];

          for (int i = 1; i < lists.length; i += 1) {
              result.plusEquals(lists[i]);
          }
          return result;
      }
}
```

What mistakes (if any) are there in `sumOfLists`? Note: The fact that the method makes the listed assumptions (lists are not null and are all of same length) is not a bug, it's an assumption.

- Return type is upcast from result, so the code will not compile.
- A 0-length array input will cause an ArrayIndexOutOfBoundsException.
- It's destructive.
- (quadratic runtime is out of scope, but acceptable answer) result.plusEquals calls the default plusEquals (in `ListOfInts`), a slower implementation which results in a quadratic runtime.

8. PNH (0 points). What two catastrophic events are believed to be responsible for the creation of almost all the gold on the earth?

- Massive meteorite shower
- Collision between neutron stars